[mex270] Anharmonic oscillator of sorts

A block of mass m with a thin but sturdy mast is bouncing back and forth between two springs of stiffness k mounted at the ends of an airtrack. Contact between block and springs begins and ends at positions $x = \pm b$.

(a) Neglect friction and dissipation during contact with springs. The block then undergoes periodic motion at constant energy E. Find the period τ of the motion as a function of E.

(b) Assume the presence of a constant kinetic frictional force f_k on the stretch between -b and +b of the track. Now the block, launched at x = 0 to the right with initial velocity v_i , comes to rest at some point on the track. Plot the final position x_f versus initial velocity v_i in a graph. Use scales in natural units of your choice along both axes.



Solution: