$[{\rm mex}191]$ Poisson's theorem

Prove Poisson's theorem for thwo dynamical variables f and g:

$$\frac{d}{dt} \left\{ f, g \right\} = \left\{ \frac{df}{dt}, g \right\} + \left\{ f, \frac{dg}{dt} \right\}.$$

Solution: