## [mex18] Rocket launch in uniform gravitational field

A rocket is launched from rest against a uniform gravitational field g by burning fuel at a constant rate,  $m = m_0(1 - \alpha t)$ . The speed of the exhaust gases relative to the rocket is u. (a) What is the minimum rate  $\alpha_{min}$  at which fuel must be burned to ensure lift-off at t = 0. (b) Calculate the velocity v(t) of the rocket and the height h(t) above ground.

## Solution: