

# Electric Field of Charged Disk



- Charge per unit area:  $\sigma = \frac{Q}{\pi R^2}$
- Area of ring:  $dA = 2\pi a da$
- Charge on ring:  $dq = 2\pi\sigma a da$
- $dE_x = \frac{kx dq}{(x^2 + a^2)^{3/2}} = \frac{2\pi\sigma k x a da}{(x^2 + a^2)^{3/2}}$
- $E_x = 2\pi\sigma k x \int_0^R \frac{ada}{(x^2 + a^2)^{3/2}} = 2\pi\sigma k x \left[ \frac{-1}{\sqrt{x^2 + a^2}} \right]_0^R$
- $E_x = 2\pi\sigma k \left[ 1 - \frac{x}{\sqrt{x^2 + R^2}} \right]$  for  $x > 0$
- $x \ll R : E_x \simeq 2\pi\sigma k$
- Infinite sheet of charge produces uniform electric field perpendicular to plane.

