Charging a capacitor requires work.

The work done is equal to the potential energy stored in the capacitor.

While charging, V increases linearly with q:

Increment of potential energy:

$$dU = V dq = \frac{q}{C} dq.$$

 $V(q) = \frac{q}{C}.$ 

Potential energy of charged capacitor:

$$U = \int_0^Q V dq = \frac{1}{C} \int_0^Q q dq = \frac{Q^2}{2C} = \frac{1}{2} C V^2 = \frac{1}{2} Q V.$$

Q: where is the potential energy stored?A: in the electric field.



