$[ext{tex}24]$ Carnot cycle of thermal radiation

Describe the four steps of a Carnot engine, where the operating material is black-body radiation. The internal energy is given by Stefan's law, $U(T,V) = \sigma T^4 V$. The equation of state is $p = \frac{1}{3}\sigma T^4$. Determine the work performance ΔW and the heat transfer ΔQ during each of the four steps and derive the Carnot efficiency from these results. Sketch the cycle in the (V,p)-plane.

Solution: