## [tex149] Square heat engine

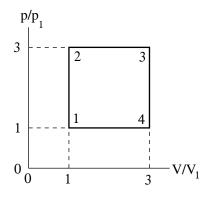
Consider 1 mol of a monatomic classical ideal gas  $[pV = RT, U = \frac{3}{2}RT]$  confined to a cylinder by a piston. The cylinder is in thermal contact with a heat bath of adjustable temperature. The gas undergoes a quasistatic, cyclic process  $1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 1$  as shown. Use  $p_1, V_1, T_1$  as units for pressure, volume, and temperature, respectively.

(a) Find  $p_2, V_2, T_2, p_3, V_3, T_3$ , and  $p_4, V_4, T_4$  in these units.

(b) Find the work performance,  $\Delta W_{12}$ ,  $\Delta W_{23}$ ,  $\Delta W_{34}$ ,  $\Delta W_{41}$ , the change in internal energy,  $\Delta U_{12}$ ,  $\Delta U_{23}$ ,  $\Delta U_{34}$ ,  $\Delta U_{41}$ , and the heat transfer,  $\Delta Q_{12}$ ,  $\Delta Q_{23}$ ,  $\Delta Q_{34}$ ,  $\Delta Q_{41}$ , along the legs of the cycle. Express these quantities in units of  $RT_1$ .

(c) Find the net work  $\Delta W_{net}$  performed during the cycle. Find also the heat  $\Delta Q_{in}$  absorbed and the heat  $\Delta Q_{out}$  expelled by the gas during the cycle.

(d) Find the efficiency  $\eta_S$  of this cycle in the role of heat engine.



Solution: