

[gex39] Duplication relation for Gamma function

Use the trigonometric integral representation of the Beta function [gmd4A] to derive the Legendre duplication relation for the Gamma function,

$$2^{2x-1}\Gamma(x)\Gamma\left(x + \frac{1}{2}\right) = \sqrt{\pi}\Gamma(2x).$$

Solution: