[lex69] Magnetic material between coaxial cylinders with currents

Consider two long coaxial cylinders with radii a, b, c as shown in cross section. They carry steady currents I with uniform current densities in opposite directions. The space between the conductors is filled with magnetic insulating material characterized by a susceptibility $\chi_{\rm m}$. Symmetry dictates that the magnetic field only has a ϕ -component (in cylindrical cordinates) and that its value only depends on r.

(a) Use Ampère's law for the **H**-field to calculate $H_{\phi}(r)$ in the four regimes (i) 0 < r < a, (ii) a < r < b, (iii) b < r < c, and (iv) r > c.

(b) Show that the bound current density is zero inside the insulating magnetic material: $\mathbf{J}_{b} = 0$. Determine the bound interface current density \mathbf{K}_{b} at r = a and at r = b.



Solution: