## [lex63] Magnetic moment of rotating charged disk

A disk of radius $R$ is uniformly charged with charge density $\sigma>0$ and rotates with angular velocity $\omega$ about its axis as shown. The rotating charge represents a current and thus produces a magnetic dipole moment $\mathbf{m}$ directed out of the plane.
(a) Express its magnitude $m$ as a function of $\omega, R$, and $Q$ (the total charge on the disk).
(b) If the disk has uniform mass density and total mass $M$, find the ratio $m / L$ of the magnetic moment and the angular momentum, also known as gyromagnetic ratio.
Hint: For part (a) split the disk into concentric rings. The current in each ring is the charge divided by the period of rotation.


## Solution:

