[lex187] Electrostatic force between two point charges

Consider two point charges $q_1 = 6nC$ and $q_2 = 4nC$ positioned at $\mathbf{x}_1 = (5\,\hat{\mathbf{i}} - 7\,\hat{\mathbf{j}} + 9\,\hat{\mathbf{k}})$ cm and $\mathbf{x}_2 = (2\,\hat{\mathbf{i}} + 3\,\hat{\mathbf{j}} - 7\,\hat{\mathbf{k}})$ cm, respectively.

(a) Express the electrostatic force acting on particle 1 in the form $\mathbf{F}_1 = F_x^{(1)} \hat{\mathbf{i}} + F_y^{(1)} \hat{\mathbf{j}} + F_z^{(1)} \hat{\mathbf{k}}$ and the electrostatic force on particle 2 in the form $\mathbf{F}_2 = (F_x^{(2)} \hat{\mathbf{i}} + F_y^{(2)} \hat{\mathbf{j}} + F_z^{(2)} \hat{\mathbf{k}})$ with numerical values for all six components in SI units.

(b) Relocate particle 1 to the position $\mathbf{x}'_1 = (x'_1 \,\hat{\mathbf{i}} + y'_1 \,\hat{\mathbf{j}} + z'_1 \,\hat{\mathbf{k}})$ such that it experiences the force $\mathbf{F}'_1 = (-5 \,\hat{\mathbf{i}} + 7 \,\hat{\mathbf{j}} + 8 \,\hat{\mathbf{k}}) \times 10^{-6}$ N. Find the three coordinates x'_1, y'_1, z'_1 in units of cm.

Solution: