[lex106] Surface charge and current in rectangular wave guide II

Consider the electric field $\mathbf{E}(\mathbf{x},t)$ and magnetic field $\mathbf{B}(\mathbf{x},t)$ of the TM(1,1) mode in a rectangular wave guide as determined in [lln18].

- (a) Infer the surface charge densities $\sigma_{\rm h}$ on the horizontal conductor (in the xz-plane) and $\sigma_{\rm v}$ on the vertical conductor (in the yz-plane).
- (b) Infer the surface current densities \mathbf{K}_h on the horizontal conductor and \mathbf{K}_v on the vertical conductor.
- (c) Establish the relations $\mathbf{K}_{\mathrm{h}} \cdot \hat{\mathbf{k}} = \sigma_{\mathrm{h}} v$, $\mathbf{K}_{\mathrm{v}} \cdot \hat{\mathbf{k}} = \sigma_{\mathrm{v}} v$, and determine the velocity v in both expressions.

Solution: