

Your Name: \_\_\_\_\_

PHY203

Exam #1  
Chapters 1-3  
Thurs, 9/30/10

# Solutions

1. The world record in swimming for the 1500 m distance is 14 min., 35 sec. What was the average speed in miles per hour?

- a. 0.064 mph       $(1.5\text{km}) \times (0.6215\text{mi/km}) / (875\text{s}) \times (3600\text{s/h}) = 3.84$   
**b. 3.84 mph**  
 c. 9.90 mph  
 d. 38.4 mph  
 e. None of the above

For questions 2-5, traveling in one direction, a train starts from rest with an acceleration of  $5 \text{ m/s}^2$  for 20 s. After 20 s, the train moves at constant speed for 50 s. Finally the train accelerates at  $-4 \text{ m/s}^2$  until it comes to rest.

2. Find the distance the train travels in the first 20 s.

- a. 50 m       $x_1 = 1/2(5 \text{ m/s}^2)(20\text{s})^2$   
 b. 100 m  
**c. 1000 m**  
 d. 2000 m  
 e. None of the above

3. Find the speed of the train after 20 s.

- a. 50 m/s       $v = (5 \text{ m/s}^2)20\text{s}$   
**b. 100 m/s**  
 c. 200 m/s  
 d. 1000 m/s  
 e. None of the above

4. Find the distance the train travels from 20 s to 70 s.

- a. 2500 m       $x_2 = (100 \text{ m/s})(50\text{s})$   
**b. 5000 m**  
 c. 10,000 m  
 d. 50,000 m  
 e. None of the above

5. Find the distance the train travels from 70 s until it comes to rest.

- a. 12.5 m       $0 = (100 \text{ m/s})^2 + 2(-4 \text{ m/s}^2)(Dx)$   
 b. 625 m  
**c. 1250 m**  
 d. 2500 m

e. None of the above

6. A bike rider rides 3 km East and then 7.5 km North. Find the magnitude of the displacement of the rider at the end of the trip.

- a. 3.2 km       $D = (3^2 + 7.5^2)^{1/2} = 8.1$   
 b. 4.5 km  
**c. 8.1 km**  
 d. 10.5 km  
 e. None of the above

7. A bike rider rides 4.5 km East and then 8.0 km North. Find the angle the displacement of the rider makes with respect to the East direction measured in a counterclockwise direction from the positive East axis at the end of the trip.

- a.  $29.4^\circ$        $q = \tan^{-1}(8/4.5) = 60.6^\circ$   
 b.  $40.4^\circ$   
**c.  $60.6^\circ$**   
 d.  $64.6^\circ$   
 e. None of the above

For problems 8-10, on Planet XXX, the acceleration due to gravity is exactly  $10 \text{ m/s}^2$ . Identical rocks are dropped from the top of a cliff. Find the time,  $t$ , at which the rocks are side-by-side.

8. Case 1: Rock a is dropped at  $t = 0$ ; rock b is dropped from the top of the cliff at  $t = 2 \text{ s}$ .

- a. 1.0 s      rock b can never catch rock a  
 b. 2.0 s  
 c. 3.0 s  
 d. 4.0 s  
**e. None of the above (never)**

9. Case 2: Rock a is dropped at  $t = 0$ ; rock b is thrown straight down at  $t = 2 \text{ s}$  with an initial speed of  $40 \text{ m/s}$ .

- a. 1.0 s       $x_a = 1/2(10)(t)^2$ ;  $x_b = 40(t-2) + 1/2(10)(t-2)^2$   
 b. 1.67 s       $x_a = x_b$ ;  $1/2(10)(t)^2 = 40(t-2) + 1/2(10)(t-2)^2$   
**c. 3.0 s**  
 d. 5.0 s  
 e. None of the above

10. Case 3: Rock a is thrown down with an initial speed of  $10 \text{ m/s}$  at  $t = 0$ ; rock b is thrown straight down at  $t = 2$  with an initial speed of  $40 \text{ m/s}$ .

- a. 1.2 s       $x_a = 10t + 1/2(10)(t)^2$ ;  $x_b = 40(t-2) + 1/2(10)(t-2)^2$   
 b. 2.0 s       $x_a = x_b$   
**c. 6.0 s**  
 d. 10.0 s  
 e. None of the above



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11. First, fill in the plots above for v vs. t and a vs. t.

**Show your work below:**

a. Find the total distance traveled from points B-H.  
distance =  $10\text{m} + 20\text{m} + 10\text{m} = 40\text{ m}$

b. Find the average speed from points B-H.  
avg. speed =  $40\text{m}/6\text{s} = 6.67\text{ m/s}$

c. Find the average velocity from points B-H.  
avg. vel. =  $(0-0)/6\text{s} = 0$

c. Find the displacement from points G-I.  
displacement =  $-10\text{m} - 10\text{m} = -20\text{ m}$

g. Find the instantaneous velocity at point H.  
slope =  $-10\text{m/s}$

h. Find the average acceleration from points C-H.

$$\text{avg. acc.} = (-10\text{m/s} - (-5\text{m/s}))/5\text{s} = -1\text{ m/s}^2$$

11. First, fill in the plots above for  $v$  vs.  $t$  and  $a$  vs.  $t$ .

**Show your work below:**

a. Find the total distance traveled from points B-H.

$$\text{distance} = 20\text{m} + 40\text{m} + 20\text{m} = 80\text{ m}$$

b. Find the average speed from points B-H.

$$\text{avg. speed} = 80\text{m}/6\text{s} = 13.3\text{ m/s}$$

c. Find the average velocity from points B-H.

$$\text{avg. vel.} = (0-0)/6\text{s} = 0$$

c. Find the displacement from points E-G.

$$\text{displacement} = -20\text{m} - 20\text{m} = -40\text{ m}$$

g. Find the instantaneous velocity at point F.

$$\text{slope} = -20\text{m/s}$$

h. Find the average acceleration from points C-F.

$$\text{avg. acc.} = (-20\text{m/s}-10\text{m/s})/3\text{s} = -10\text{ m/s}^2$$

12. A boy who is standing on top of a 30 m tall building throws a ball at a nearby building that is 100 m tall. The initial velocity in the  $x$ -direction given to the ball is 30 m/s. When the ball hits the top, left corner of the building, it is at the highest point of its trajectory. Use  $g = 9.81\text{ m/s}^2$ .



**Show your work below:**

a. Calculate the initial velocity of the ball in the  $y$ -direction.

$$0 = (v_{y0})^2 - 2(9.81 \text{ m/s}^2)(100\text{m} - 30\text{m})$$

$$v_{y0} = + 37 \text{ m/s}$$

b. Calculate the initial speed of the ball.

$$v = (30^2 + 37^2)^{1/2} = 47.6 \text{ m/s}$$

c. Calculate the angle the ball made initially with respect to the horizontal (x) direction.

$$q = \tan^{-1}(37/30) = 51^\circ$$

d. Write the initial velocity in vector notation using the coordinate system shown above.

$$\mathbf{v}_0 = (\underline{\quad 30 \quad} \mathbf{i} + \underline{\quad 37 \quad} \mathbf{j}) \text{ m/s}$$

e. Calculate the time it takes for the ball to reach the roof of the second building.

$$0 = 37 \text{ m/s} - (9.81 \text{ m/s}^2)(t)$$

$$t = 3.8\text{s}$$

f. Find the velocity of the ball just as it is hitting the roof and write it in vector notation using the coordinate system shown above.

$$\mathbf{v} = 30 \text{ m/s } \mathbf{i}$$

12. A boy who is standing on top of a 30 m tall building throws a ball at a nearby building that is 100 m tall. The initial velocity in the x-direction given to the ball is 40 m/s. When the ball hits the top, left corner of the building, it is at the highest point of its trajectory. Use  $g = 9.81 \text{ m/s}^2$ .



**Show your work below:**

a. Calculate the initial velocity of the ball in the y-direction.

$$0 = (v_{y0})^2 - 2(9.81 \text{ m/s}^2)(100\text{m} - 30\text{m})$$

$$v_{y0} = + 37 \text{ m/s}$$

b. Calculate the initial speed of the ball.

$$v = (40^2 + 37^2)^{1/2} = 54.5 \text{ m/s}$$

c. Calculate the angle the ball made initially with respect to the horizontal (x) direction.

$$q = \tan^{-1}(37/40) = 42.8^\circ$$

d. Write the initial velocity in vector notation using the coordinate system shown above.

$$\mathbf{v}_0 = (\underline{\quad 40 \quad} \mathbf{i} + \underline{\quad 37 \quad} \mathbf{j}) \text{ m/s}$$

e. Calculate the time it takes for the ball to reach the roof of the second building.

$$0 = 37 \text{ m/s} - (9.81 \text{ m/s}^2)(t)$$
$$t = 3.77 \text{ s}$$

f. Find the velocity of the ball just as it is hitting the roof and write it in vector notation using the coordinate system shown above.

$$\mathbf{v} = 40 \text{ m/s } \mathbf{i}$$