

Your Name: \_\_\_\_\_

PHY203  
Final Exam  
Mon., 12/16/13

# Part 1

# Solutions

1. Ball A is dropped from the edge of the top of a cliff of height 250 m. After a delay of 2.00 s, ball B is thrown straight down with some initial speed. (Ignore air resistance.) Take "up" as the positive x-direction with  $x=0$  at the base of the cliff.
- a. Find the time at which ball A reaches the bottom of the cliff.

Use kinematic eq. A:

**15**

$$0 = 250 \text{ m} + (0)(t) + 1/2(-9.81 \text{ m/s}^2)(t)^2$$

$$t = 7.14 \text{ s}$$

- b. Find the speed of ball A just before it reaches the bottom of the cliff.

$$v_y = 0 + (-9.81 \text{ m/s}^2)(7.14 \text{ s})$$

**10**

$$\text{speed} = +70.0 \text{ m/s}$$

- c. Assuming that the two balls reach the bottom of the cliff at the same time, find the initial velocity (magnitude and sign) of ball B.

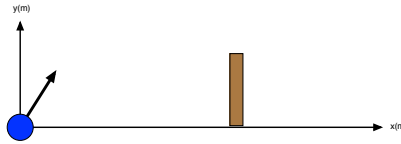
For ball B:

Use kinematic eq. A:

**25**

$$0 = 250 \text{ m} + (v_B)(5.14 \text{ s}) + 1/2(-9.81 \text{ m/s}^2)(5.14)^2$$

$$v_B = -23.4 \text{ m/s}$$



2. A cannon ball is launched with an *x*-component of initial speed of 22.0 m/s at a 15.0 m high wall that is 55.0 m from the cannon. The ball just grazes the top of the wall *on the way down*. (Ignore air resistance.)

a. Find the time it takes the ball to reach the wall.

Use kinematic eq. A:

**15**

$$55.0 \text{ m} = 0 + (22.0 \text{ m/s})(t) + 0$$

$$t = 2.50 \text{ s}$$

b. Find the magnitude of the *y* component of the initial velocity of the ball.

Use kinematic eq. A:

**15**

$$15.0 \text{ m} = 0 + (v_y)(2.50 \text{ s}) + 1/2(-9.81 \text{ m/s}^2)(2.50)^2$$

$$v_y = 18.3 \text{ m/s}$$

c. Find the *y*-component of the velocity of the ball when it hits the wall using the above coordinate system.

$$v_y = 18.3 \text{ m/s} + (-9.81 \text{ m/s}^2)(2.50 \text{ s})$$

**15**

$$v_y = -6.22 \text{ m/s}$$

d. Find the magnitude the velocity at that point.

$$v = \sqrt{v_x^2 + v_y^2} = \sqrt{(22.0 \text{ m/s})^2 + (-6.22 \text{ m/s})^2}$$

**5**

$$= 22.9 \text{ m/s}$$

Alternate

1. Ball A is dropped from the edge of the top of a cliff of height 350 m. After a delay of 3.00 s, ball B is thrown straight down with some initial speed. (Ignore air resistance.) Take "up" as the positive x-direction with  $x=0$  at the base of the cliff.
- a. Find the time at which ball A reaches the bottom of the cliff.

Use kinematic eq. A:

**15**

$$0 = 350 \text{ m} + (0)(t) + 1/2(-9.81 \text{ m/s}^2)(t)^2$$

$$t = 8.45 \text{ s}$$

- b. Find the speed of ball A just before it reaches the bottom of the cliff.

$$v_y = 0 + (-9.81 \text{ m/s}^2)(8.45 \text{ s})$$

**10**

$$\text{speed} = +82.9 \text{ m/s}$$

- c. Assuming that the two balls reach the bottom of the cliff at the same time, find the initial velocity (magnitude and sign) of ball B.

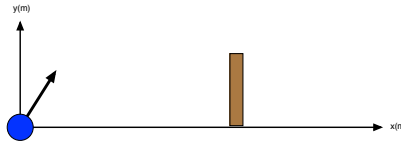
For ball B:

Use kinematic eq. A:

**25**

$$0 = 350 \text{ m} + (v_B)(5.45 \text{ s}) + 1/2(-9.81 \text{ m/s}^2)(5.45)^2$$

$$v_B = -37.5 \text{ m/s}$$



2. A cannon ball is launched with an *x*-component of initial speed of 20.0 m/s at a 18.0 m high wall that is 65.0 m from the cannon. The ball just grazes the top of the wall *on the way down*. (Ignore air resistance.)

a. Find the time it takes the ball to reach the wall.

Use kinematic eq. A:

**15**

$$65.0 \text{ m} = 0 + (20.0 \text{ m/s})(t) + 0$$

$$t = 3.25 \text{ s}$$

b. Find the magnitude of the *y* component of the initial velocity of the ball.

Use kinematic eq. A:

**15**

$$18.0 \text{ m} = 0 + (v_y)(3.25 \text{ s}) + 1/2(-9.81 \text{ m/s}^2)(3.25)^2$$

$$v_y = 21.5 \text{ m/s}$$

c. Find the *y*-component of the velocity of the ball when it hits the wall using the above coordinate system.

$$v_y = 21.5 \text{ m/s} + (-9.81 \text{ m/s}^2)(3.25 \text{ s})$$

**15**

$$v_y = -10.4 \text{ m/s}$$

d. Find the magnitude the velocity at that point.

$$v = \sqrt{v_x^2 + v_y^2} = \sqrt{(20.0 \text{ m/s})^2 + (-10.4 \text{ m/s})^2}$$

**5**

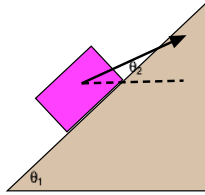
$$= 22.5 \text{ m/s}$$

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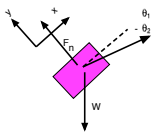
PHY203  
Final Exam #2  
Fri., 5/10/13

# Part 2

# Solutions



1. A 3.50 kg block is being pushed up a frictionless ramp by a force of  $F = 45.0$  N.  
 a. Draw a free-body diagram (sketch and label all the forces on the block).  
*Include a coordinate system.*



**10**

- b. Take  $\theta_1 = 50^\circ$  and  $\theta_2 = 30^\circ$   
 Write out Newton's 2nd Law for the block for both axes. (*Don't solve the equations yet.*)

y-direction:  $F_n - mg \cos \theta_1 - F \sin(\theta_1 - \theta_2) = 0$  **10**

x-direction:  $F \cos(\theta_1 - \theta_2) - mg \sin \theta_1 = ma$  **10**

- c. Find the magnitude of the acceleration of the block.

$$a = \frac{F \cos(\theta_1 - \theta_2) - mg \sin \theta_1}{m}$$

$$= \frac{(45.0) \cos 20^\circ - (3.50)(9.81) \sin 50^\circ}{3.50} \quad \mathbf{10}$$

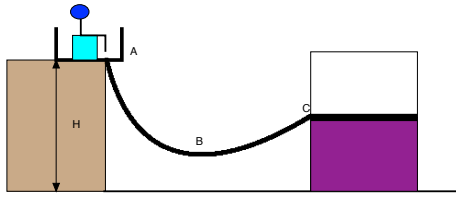
$$= 4.57 \text{ m/s}^2$$

- d. Find the magnitude of the normal force on the block.

$$F_n = mg \cos \theta_1 + F \sin(\theta_1 - \theta_2)$$

$$= (3.5)(9.81) \cos(50^\circ) + (45.0) \sin(20^\circ) \quad \mathbf{10}$$

$$= 37.5 \text{ N}$$



2. A roller coaster is at rest at the top of its track at point A, which is at a height of  $H_A = 150$  m. The rollercoaster rolls off the track and descends. The mass of the car is 100 kg; the mass of the rider is 75.0 kg.
- a. Find the speed of the rollercoaster at point B, with  $H_B = 60.0$  m.

$$E = mgh_A = mgh_B + \frac{1}{2}mv^2$$

$$v^2 = 2g(h_A - h_B) = 2(9.81)(150 - 60.0)$$

**10**

$$v = 42.0 \text{ m/s}$$

- b. Draw a free-body diagram of a person sitting in the roller coaster when it gets to point B.



**5**

- c. Find the magnitude of the force of the chair on the person at point B. Assume at point B that the section of track is part of a circle of radius 35.0 m.

$$F_n - mg = \frac{mv^2}{r}$$

$$F_n = \frac{mv^2}{r} + mg = \frac{(75.0)(42.0)^2}{35.0} + (75.0)(9.81)$$

**15**

$$= 4.52 \times 10^3 \text{ N}$$

- d. Find the work that went into friction along the rough section of track from B to C assuming that the speed of the rollercoaster at point C is 25.0 m/s, with  $H_C = 110$  m.

$$E = mgh_A = mgh_C + \frac{1}{2}mv^2 + W_f$$

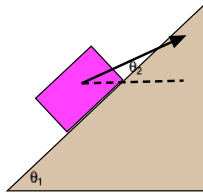
$$W_f = mg(h_A - h_C) - \frac{1}{2}mv^2$$

**20**

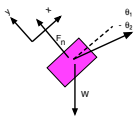
$$= (175)(9.81)(150 - 110) - \frac{1}{2}(175)(25.0)^2$$

$$= 1.40 \times 10^4 \text{ J}$$

Alternate



1. A 4.50 kg block is being pushed up a frictionless ramp by a force of  $F = 55.0$  N.  
a. Draw a free-body diagram (sketch and label all the forces on the block).  
*Include a coordinate system.*



**10**

- b. Take  $\theta_1 = 50^\circ$  and  $\theta_2 = 30^\circ$   
Write out Newton's 2nd Law for the block for both axes. (*Don't solve the equations yet.*)

y-direction:  $F_n - mg\cos\theta_1 - F\sin(\theta_1 - \theta_2) = 0$  **10**

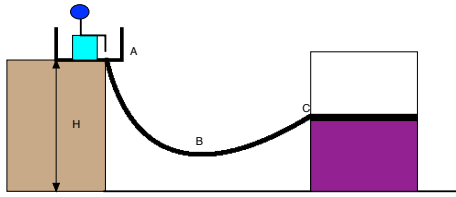
x-direction:  $F\cos(\theta_1 - \theta_2) - mg\sin\theta_1 = ma$  **10**

- c. Find the magnitude of the acceleration of the block.

$$\begin{aligned} a &= \frac{F\cos(\theta_1 - \theta_2) - mg\sin\theta_1}{m} \\ &= \frac{(55.0)\cos 20^\circ - (4.50)(9.81)\sin 50^\circ}{4.50} \quad \mathbf{10} \\ &= 3.97 \text{ m/s}^2 \end{aligned}$$

- d. Find the magnitude of the normal force on the block.

$$\begin{aligned} F_n &= mg\cos\theta_1 + F\sin(\theta_1 - \theta_2) \\ &= (4.5)(9.81)\cos(50^\circ) + (55.0)\sin(20^\circ) \quad \mathbf{10} \\ &= 47.2 \text{ N} \end{aligned}$$



2. A roller coaster is at rest at the top of its track at point A, which is at a height of  $H_A = 200$  m. The rollercoaster rolls off the track and descends. The mass of the car is 100 kg; the mass of the rider is 75.0 kg.
- a. Find the speed of the rollercoaster at point B, with  $H_B = 80.0$  m.

$$E = mgh_A = mgh_B + \frac{1}{2}mv^2$$

$$v^2 = 2g(h_A - h_B) = 2(9.81)(200 - 80.0)$$

**10**

$$v = 48.5 \text{ m/s}$$

- b. Draw a free-body diagram of a person sitting in the roller coaster when it gets to point B.



**5**

- c. Find the magnitude of the force of the chair on the person at point B. Assume at point B that the section of track is part of a circle of radius 45.0 m.

$$F_n - mg = \frac{mv^2}{r}$$

$$F_n = \frac{mv^2}{r} + mg = \frac{(75.0)(48.5)^2}{45.0} + (75.0)(9.81)$$

**15**

$$= 4.66 \times 10^3 \text{ N}$$

- d. Find the work that went into friction along the rough section of track from B to C assuming that the speed of the rollercoaster at point C is 25.0 m/s, with  $H_C = 140$  m.

$$E = mgh_A = mgh_C + \frac{1}{2}mv^2 + W_f$$

$$W_f = mg(h_A - h_C) - \frac{1}{2}mv^2$$

**20**

$$= (175)(9.81)(200 - 140) - \frac{1}{2}(175)(25.0)^2$$

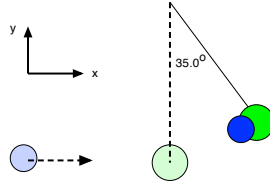
$$= 4.83 \times 10^4 \text{ J}$$

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PHY203  
Final Exam #3  
Fri., 5/10/13

# Part 3

# Solutions



1. A 2.50 kg ball traveling in the positive x-direction collides with and sticks to a 3.50 kg ball that is suspended from a string of length 0.750 m. The balls stick together and swing up to a maximum angle of 35.0°, as shown above.

a. Find the maximum change in height of the 2-ball combination.

$$h = L(1 - \cos\theta) = (0.750\text{m})(1 - \cos 35^\circ) = 0.136\text{m} \quad \mathbf{10}$$

b. Using conservation of energy, find the speed of the 2-ball combination just after the collision.

$$K_i = mgh$$

$$\frac{1}{2}m(v)^2 = mgh \quad \mathbf{15}$$

$$v = \sqrt{2gh} = \sqrt{2g(0.136\text{m})} = 1.63\text{m/s}$$

c. Find the momentum of the 2-ball combination just after the collision and write it in vector notation.

$$\mathbf{p} = (6.00)(1.63) = 9.80\text{kgm/si} \quad \mathbf{10}$$

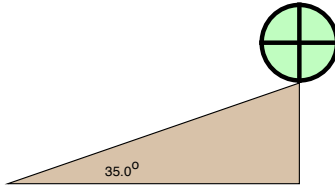
d. Find the momentum of the 2.50 kg ball just before the collision and write it in vector notation.

$$\text{same} = 9.80\text{kgm/si} \quad \mathbf{5}$$

e. Find the speed of the 2.50 kg ball just before the collision.

$$9.80\text{kgm/s} = (2.50\text{kg})v$$

$$v = 3.92\text{m/s} \quad \mathbf{10}$$



2. A wheel which is a rim of mass 1.50 kg and radius 0.650 with 4 spokes of mass 0.500 kg is being held at the top of a ramp which has a length of 2.50 m and an angle of  $35^\circ$ .

a. Find the moment of inertia of the wheel about its axis.

$$I = (1.50\text{kg})(0.650\text{m})^2 + 4\left(\frac{1}{3}(0.500\text{kg})(0.650\text{m})^2\right) = 0.915\text{kgm}^2 \quad \mathbf{10}$$

b. Find the change in potential energy of the wheel from the top of the ramp to the floor level.

$$\Delta U = mgh = (3.50)(9.81)(2.50)\sin(35^\circ) = 49.2\text{J} \quad \mathbf{10}$$

c. Use conservation of energy to find the speed of the wheel at the bottom of the ramp.

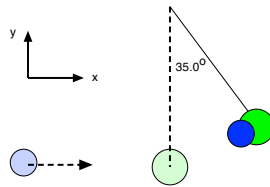
$$\Delta U = 49.2\text{J} = K_f$$

$$49.2\text{J} = \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2 = \frac{1}{2}mv^2 + \frac{1}{2}I\left(\frac{v}{r}\right)^2 \quad \mathbf{30}$$

$$= \frac{1}{2}v^2\left(m + I\left(\frac{1}{r}\right)^2\right) = \frac{1}{2}v^2\left(3.50 + (0.916)\left(\frac{1}{0.650}\right)^2\right)$$

$$v = 4.17\text{m/s}$$

Alternate



1. A 3.50 kg ball traveling in the positive x-direction collides with and sticks to a 4.50 kg ball that is suspended from a string of length 0.850 m. The balls stick together and swing up to a maximum angle of  $35.0^\circ$ , as shown above.

a. Find the maximum change in height of the 2-ball combination.

$$h = L(1 - \cos \theta) = (0.850\text{m})(1 - \cos 35^\circ) = 0.154\text{m} \quad \mathbf{10}$$

b. Using conservation of energy, find the speed of the 2-ball combination just after the collision.

$$K_i = mgh$$
$$\frac{1}{2}m(v)^2 = mgh \quad \mathbf{15}$$
$$v = \sqrt{2gh} = \sqrt{2g(0.154\text{m})} = 1.74\text{m/s}$$

c. Find the momentum of the 2-ball combination just after the collision and write it in vector notation.

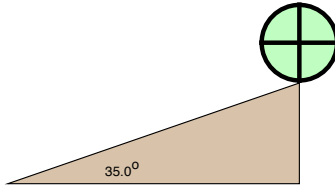
$$\mathbf{p} = (8.00)(1.74) = 13.9\text{kgm/s} \quad \mathbf{10}$$

d. Find the momentum of the 2.50 kg ball just before the collision and write it in vector notation.

$$\text{same} = 13.9\text{kgm/s} \quad \mathbf{5}$$

e. Find the speed of the 2.50 kg ball just before the collision.

$$13.9\text{kgm/s} = (3.50\text{kg})v$$
$$v = 3.97\text{m/s} \quad \mathbf{10}$$



2. A wheel which is a rim of mass 2.50 kg and radius 0.750 with 4 spokes of mass 0.750 kg is being held at the top of a ramp which has a length of 3.50 m and an angle of  $35^\circ$ .

a. Find the moment of inertia of the wheel about its axis.

$$I = (2.50\text{kg})(0.750\text{m})^2 + 4\left(\frac{1}{3}(0.750\text{kg})(0.750\text{m})^2\right) = 1.97\text{kgm}^2 \quad \mathbf{10}$$

b. Find the change in potential energy of the wheel from the top of the ramp to the floor level.

$$\Delta U = mgh = (5.50)(9.81)(3.50)(\sin(35^\circ)) = 108\text{J} \quad \mathbf{10}$$

c. Use conservation of energy to find the speed of the wheel at the bottom of the ramp.

$$\begin{aligned} \Delta U = 108\text{J} &= K_f \\ 108\text{J} &= \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2 = \frac{1}{2}mv^2 + \frac{1}{2}I\left(\frac{v}{r}\right)^2 \\ &= \frac{1}{2}v^2\left(m + I\left(\frac{1}{r}\right)^2\right) = \frac{1}{2}v^2\left(5.5 + (1.97)\left(\frac{1}{0.750}\right)^2\right) \\ v &= 4.90\text{m/s} \end{aligned} \quad \mathbf{30}$$

Your Name: \_\_\_\_\_

PHY203  
Final Exam #4  
Fri., 5/10/13

# Part 4

# Solutions

1. A planet has a mass of  $3.50 \times 10^{26}$  kg and a radius of  $2.00 \times 10^3$  km.  
 a. Find the magnitude of the force of gravity on a 550 kg satellite at a height of  $1.5 \times 10^3$  km above the planet's surface.

$$F = \frac{GmM}{R^2} = \frac{(6.67 \times 10^{-11})(550)(3.50 \times 10^{26})}{(3.50 \times 10^6 \text{ m})^2} = 1.05 \times 10^6 \text{ N} \quad \mathbf{10}$$

- b. Find the speed of a 550 kg satellite in orbit at that height.

$$F_c = \frac{mv^2}{r} \quad \mathbf{10}$$

$$v = \sqrt{\frac{F_c r}{m}} = \sqrt{\frac{(1.05 \times 10^6)(3.50 \times 10^6 \text{ m})}{550}} = 8.17 \times 10^4 \text{ m/s}$$

- c. Find the period of the orbit.

$$T = \frac{2\pi r}{v} = \frac{2\pi(3.50 \times 10^6 \text{ m})}{8.17 \times 10^4} = 269 \text{ s} \quad \mathbf{10}$$

- d. If the 550 kg satellite falls out of this orbit, find the speed of the satellite when it hits the surface of the planet assuming it started from rest.

$$-\frac{mGM}{R+h} = +\frac{1}{2}mv^2 - \frac{mGM}{R} \quad \mathbf{20}$$

$$v^2 = \frac{2GM}{R} \left[ 1 - \frac{1}{1+h/R} \right]$$

$$= \frac{2(6.67 \times 10^{-11})(3.50 \times 10^{26})}{(2.00 \times 10^6 \text{ m})} \left[ 1 - \frac{1}{1+(1.50)/(2.00)} \right]$$

$$v = 1.00 \times 10^5 \text{ m/s}$$

2. A block is attached to a spring with spring constant 500 N/m. The block is stretched and released. The equation of motion of the block is as follows (with x in meters):

$$x(t) = (0.550)\cos(7.50t)$$

a. Find the period of the system.

$$T = \frac{2\pi}{\omega} = \frac{2\pi}{7.50} = 0.838s \quad \mathbf{5}$$

b. Find the mass of the block.

$$\omega = \sqrt{\frac{k}{m}} \quad \mathbf{10}$$

$$m = \frac{k}{\omega^2} = \frac{500}{(7.50)^2} = 8.89kg$$

c. Find the total energy of the system.

$$E = \frac{1}{2}kA^2 = \frac{1}{2}(500)(0.550)^2 = 75.6J \quad \mathbf{5}$$

d. Find the first time at which the block is at a position of x = 0.350 m.

$$0.350 = (0.550)\cos(7.50t) \quad \mathbf{15}$$

$$t = 0.117 s$$

e. Find (and show work) in what direction the block is traveling at that time.

$$v = \frac{dx}{dt} = -\omega A \sin(\omega t)$$

$$v(0.117) = \frac{dx}{dt} = -(7.50)(0.550)\sin(7.50 \times 0.117) \quad \mathbf{15}$$

$$= -3.17m/s$$

so negative x-direction

Alternate

1. A planet has a mass of  $4.50 \times 10^{26}$  kg and a radius of  $3.00 \times 10^3$  km.  
a. Find the magnitude of the force of gravity on a 650 kg satellite at a height of  $2.5 \times 10^3$  km above the planet's surface.

$$F = \frac{GmM}{R^2} = \frac{(6.67 \times 10^{-11})(650)(4.50 \times 10^{26})}{(5.50 \times 10^6 \text{ m})^2} = 6.45 \times 10^5 \text{ N} \quad \mathbf{10}$$

- b. Find the speed of a 650 kg satellite in orbit at that height.

$$F_c = \frac{mv^2}{r} \quad \mathbf{10}$$
$$v = \sqrt{\frac{F_c r}{m}} = \sqrt{\frac{(6.45 \times 10^5)(5.50 \times 10^6 \text{ m})}{650}} = 7.39 \times 10^4 \text{ m/s}$$

- c. Find the period of the orbit.

$$T = \frac{2\pi r}{v} = \frac{2\pi(5.50 \times 10^6 \text{ m})}{7.39 \times 10^4} = 468 \text{ s} \quad \mathbf{10}$$

- d. If the 550 kg satellite falls out of this orbit, find the speed of the satellite when it hits the surface of the planet assuming it started from rest.

$$-\frac{mGM}{R+h} = +\frac{1}{2}mv^2 - \frac{mGM}{R} \quad \mathbf{20}$$
$$v^2 = \frac{2GM}{R} \left[ 1 - \frac{1}{1+h/R} \right]$$
$$= \frac{2(6.67 \times 10^{-11})(4.50 \times 10^{26})}{(3.00 \times 10^6 \text{ m})} \left[ 1 - \frac{1}{1+(2.50)/(3.00)} \right]$$
$$v = 9.54 \times 10^4 \text{ m/s}$$

2. A block is attached to a spring with spring constant 600 N/m. The block is stretched and released. The equation of motion of the block is as follows (with x in meters):

$$x(t) = (0.650)\cos(5.50t)$$

a. Find the period of the system.

$$T = \frac{2\pi}{\omega} = \frac{2\pi}{5.50} = 1.14s \quad \mathbf{5}$$

b. Find the mass of the block.

$$\omega = \sqrt{\frac{k}{m}} \quad \mathbf{10}$$

$$m = \frac{k}{\omega^2} = \frac{600}{(5.50)^2} = 19.8kg$$

c. Find the total energy of the system.

$$E = \frac{1}{2}kA^2 = \frac{1}{2}(600)(0.650)^2 = 127J \quad \mathbf{5}$$

d. Find the first time at which the block is at a position of x = 0.250 m.

$$0.250 = (0.650)\cos(5.50t) \quad \mathbf{15}$$

$$t = 0.213 s$$

e. Find (and show work) in what direction the block is traveling at that time.

$$v = \frac{dx}{dt} = -\omega A \sin(\omega t)$$

$$v(0.213) = \frac{dx}{dt} = -(5.50)(0.650)\sin(5.50 \times 0.213) \quad \mathbf{15}$$

$$= -3.30m/s$$

so negative x-direction