

Your Name: _____

PHY203
Final Exam
Chapters 1-11,15

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wedi, May 8, 2024

- Show work
- Use correct SI units
- Use scientific notation
- All answers with 3 significant figures
- use $g = 9.81 \text{ m/s}^2$

Solutions

Makeup Final F23

1. A car passes $x=0$ at $t=0$ traveling in the $+x$ direction with a constant speed of 15.0 m/s. It travels at this speed for 25.0 s, then it accelerates in the $+x$ direction with a magnitude of 3.00 m/s² for an additional 35.0 s. Finally, it slows down until coming to rest with an acceleration of magnitude 2.25 m/s².

a. For the first 25.0 s, fill out the table below:

Parameter	Known Value
x_0	0
x_f	
v_0	15.0 m/s
v_f	15.0 m/s
a	0
t	25.0 s

b. Find the distance the car has traveled after 25.0 s. 10

$$x = 0 + 15.0(25.0) + 0 = 375 \text{ m}$$

c. For the 25.0 s to 60.0 s, fill out the table below:

Parameter	Known Value
x_0	375 m
x_f	
v_0	15.0 m/s
v_f	
a	3.00 m/s ²
t	35.0 s

d. Find the speed of the car after 60.0 s. 10

$$v = 15.0 + 3.00(35.00) = 120 \text{ m/s}$$

e. Find the total distance the car has traveled after 60.0 s. 10

$$x = 375 + 15.0(35.0) + \frac{1}{2}(3.00)(35.0)^2 = 2.74 \times 10^3 \text{ m}$$

f. For the period of 60.0 s to when it stops, fill out the table below:

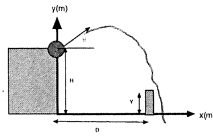
Parameter	Known Value
x_0	2737.5 m
x_f	
v_0	120 m/s
v_f	0
a	-2.25 m/s ²
t	

g. Find the total time the car has been traveling before it comes to rest. 10

$$0 = 120 - 2.25t \Rightarrow t = 53.3 \text{ s} + 60 = 113 \text{ s}$$

h. Find the total distance the car has traveled when it has come to rest. 10

$$x = 2737.5 + 120(53.3) - \frac{1}{2}(2.25)(53.3)^2 = 5.94 \times 10^3 \text{ m}$$



2. A cannonball is shot from a cliff of height $H = 115 \text{ m}$ at a castle wall, as shown above. The castle wall is $Y = 55.0 \text{ m}$ high and a horizontal distance $D = 205 \text{ m}$ from the cannon. Take $y = 0$ at ground level.

Assume the ball just grazes the top of the wall after traveling for 6.75 s

a. On the figure above, plot the trajectory of the cannonball. **5**

b. Fill out the tables of known values.

Take the final position as when the cannonball grazes the castle wall.

Parameter	Known Value
x_0	0
x_f	205 m
v_{x0}	
v_{xf}	
a_x	0
t	6.75 s

Parameter	Known Value
y_0	115 m
y_f	55.0 m
v_{y0}	
v_{yf}	
a_y	-9.81 m/s^2
t	6.75 s

c. Find the initial velocity of the cannonball and write it in vector notation using the coordinate system above. **20**

$$x: 205 = 0 + v_{x0}(6.75) + 0$$

$$v_{x0} = 30.3 \text{ m/s}$$

$$y: 55.0 = 115 + v_{y0}(6.75) - \frac{1}{2}g(6.75)^2$$

$$v_{y0} = 24.2 \text{ m/s}$$

$$\vec{v}_0 = (30.3\hat{i} + 24.2\hat{j}) \text{ m/s}$$

d. Find the acceleration, velocity, and position of the cannonball in vector notation just before it hits the ground on the other side of the wall. **25**

$$\vec{a} = -9.81\hat{j} \text{ m/s}^2$$

$$y: 0 = 115 + 24.2t - \frac{1}{2}gt^2$$

$$4.905t^2 - 24.2t - 115 = 0$$

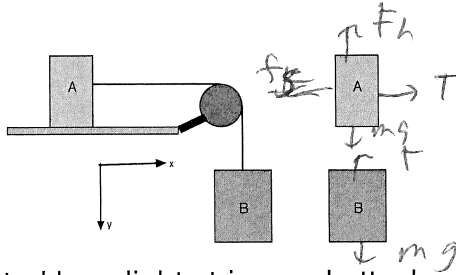
$$t = \frac{24.2 \pm \sqrt{4.905t^2 + 4(4.905)(115)}}{9.81} = 7.90 \text{ s}$$

$$v_y = 24.2 + at = 24.2 - g(7.90) = -53.3 \text{ m/s}$$

$$\vec{v} = (30.3\hat{i} - 53.3\hat{j}) \text{ m/s}$$

$$x: x = 0 + 30.3(7.90) = 239 \text{ m}$$

$$\vec{r} = 239\hat{i} \text{ m}$$



3. Blocks A and B are connected by a light string and attached over a massless pulley and are initially at rest. Assume a rough surface under block A with coefficient of static friction μ_s and masses M_A and M_B . The blocks are released and are just about to start sliding.

a. Draw free body diagrams on the blocks shown above and on the right. 5

b. Write out Newton's 2nd Law for both blocks in x- and y-directions. 30

$$\begin{aligned}
 \text{A: } & \begin{aligned}
 x: & T - f_{s \max} = m_A a = 0 \\
 y: & m_A g - F_n = 0
 \end{aligned} \\
 \text{B: } & \begin{aligned}
 y: & m_B g - T = m_B a = 0
 \end{aligned}
 \end{aligned}$$

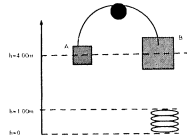
Assume that $M_A = 9.50 \text{ kg}$, $M_B = 7.50 \text{ kg}$.

c. Find the coefficient of static friction. 15

$$\text{Combine: } m_B g - f_{s \max} = 0$$

$$m_B g = \mu_s F_n = \mu_s m_A g$$

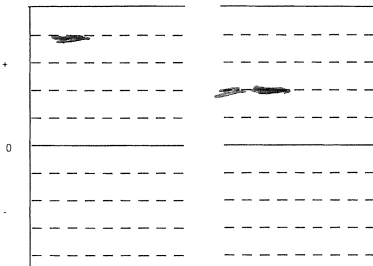
$$\mu_s = \frac{m_B g}{m_A g} = \frac{7.50}{9.50} = 0.789$$



4. Two blocks with masses m_A and m_B are connected by a light string and suspended over a massless pulley. Assume the initial height of both blocks is $h = 4.00$ m. The blocks are released. (Ignore the size of the blocks.) We want to find the speeds of the blocks after they have traveled 3.00 m. At 3.00 m block B just makes contact with the spring, which is still uncompressed at that point.

a. Create energy bar charts: **5**

$K, U_{\text{grav}}, U_{\text{spring}}, E_{\text{th}}$ $K, U_{\text{grav}}, U_{\text{spring}}, E_{\text{th}}$



b. Assume $m_A = 5.00$ kg and $m_B = 7.50$ kg. Find the initial energy of the blocks before they start moving. **5**

$$U_g = (5.00 + 7.50)g(4.00) = 490 \text{ J}$$

c. Use Conservation of Energy to find the speeds of the blocks after they have traveled 3.00 m. **20**

$$490.5 = \frac{1}{2} (12.5) v^2 + g [5.7 + 7.5 \cdot 1]$$

$$= 6.25 v^2 + 414.9$$

$$6.25 v^2 = 73.4$$

$$v = 3.43 \text{ m/s}$$

d. After block B has traveled 3.00 m (and is just touching the spring), the string breaks and the block lands on the spring which has a spring constant of $k = 800$ N/m. Find the maximum compression of the spring. **20**

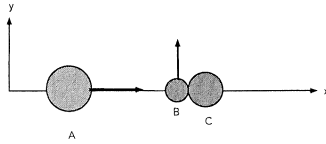
$$\frac{1}{2} m v_B^2 = \frac{1}{2} k d^2 - m g d$$

$$\frac{1}{2} (7.5) (3.43)^2 = \frac{800}{2} d^2 - (7.5)g(d)$$

$$0 \quad 44.1 = 400d^2 - 73.6d - 44.1$$

$$d = \frac{73.6 \pm \sqrt{73.6^2 + 4 \cdot 400 \cdot 44.1}}{800}$$

$$= 0.237 \text{ m}$$



5. A disk (A) of mass 8.50 kg is traveling on a frictionless surface in the +x direction with a speed of 12.5 m/s. At $t=0$, the disk breaks into 2 pieces, B and C. Piece B (mass of 5.00 kg) travels off in the +y-direction with a speed of 9.50 m/s.

a. List the known quantities before and after the breakup:

Parameter	Known Value
M_A	8.50 kg
V_A	12.5 m/s \hat{i}

Parameter	Known Value
M_B	5.00 kg
V_B	9.50 m/s \hat{j}
M_C	3.50 kg

b. Find the linear momentum of disk A before the breakup and write it in vector notation. **10**

10

$$\vec{p}_A = (8.50)(12.5) \hat{i} = 106 \text{ kg m/s } \hat{i}$$

c. Find the linear momentum of piece B after the breakup and in vector notation. **10**

$$\vec{p}_B = (5.00)(9.50) \hat{j} = 47.5 \text{ kg m/s } \hat{j}$$

d. Find the velocity of piece C after the breakup and write it in vector notation. **20**

$$106 \hat{i} = 47.5 \hat{j} + (v_{Cx} \hat{i} + v_{Cy} \hat{j})(3.50)$$

$$x^\circ: 106 = 3.50 v_{Cx}; v_{Cx} = 30.3 \text{ m/s}$$

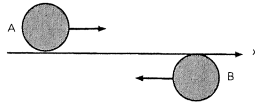
$$y^\circ: 0 = 47.5 + v_{Cy}(3.5); v_{Cy} = -13.6 \text{ m/s}$$

$$\vec{v}_C = (30.3 \hat{i} - 13.6 \hat{j}) \text{ m/s}$$

e. Find the angle the velocity of piece C makes with the x-axis. **10**

$$\theta = \tan^{-1}\left(\frac{v_y}{v_x}\right) = \tan^{-1}\left(\frac{-13.6}{30.3}\right) = -24.1^\circ$$

(or 336°)



6. Two disks of radius 0.750 m and mass 0.500 kg are traveling towards each other with speeds of 4.50 m/s, as shown above. When the disks touch, the disks stick together and they start rotating without any further translation. A sketch of the initial situation including a coordinate system is given above. Take the +z-axis as out of the paper.

a. Sketch the final situation as the sticks are rotating about a common center. **5**



b. Find the linear momenta of disks A and B before the collision and write them in vector notation. **10**

$$\vec{p}_A = (0.500)(4.50)\vec{i} = 2.25\vec{i} \text{ kg m/s}$$

$$\vec{p}_B = (0.500)(-4.50)\vec{i} = -2.25\vec{i} \text{ kg m/s}$$

c. Find the angular momentum of the 2-disk system in vector notation about the collision point before the collision. (Hint: you can treat the disks as point masses for this calculation.) **15**

$$\vec{L}_A = \vec{r} \times \vec{p} = r m v = (0.75)(2.25) \quad \vec{r} \perp \vec{p}$$

$$= -1.69 \text{ kg m}^2/\text{s} \vec{k} = \vec{L}_B$$

$$\vec{L}_{\text{tot}} = -3.38 \text{ kg m}^2/\text{s} \vec{k}$$

d. Find the moment of inertia of the 2-disk system just after the collision. (Hint: you can treat the disks as point masses for this calculation.) **10**

$$I = 2(m r^2) = 2(0.500)(0.750)^2$$

$$= 0.5625 \text{ kg m}^2$$

e. Find the angular speed of the 2-disk system just after the collision. **10**

$$L = I\omega$$

$$3.38 = 0.5625 \omega$$

$$\omega_f = 6.01 \text{ rad/s}$$