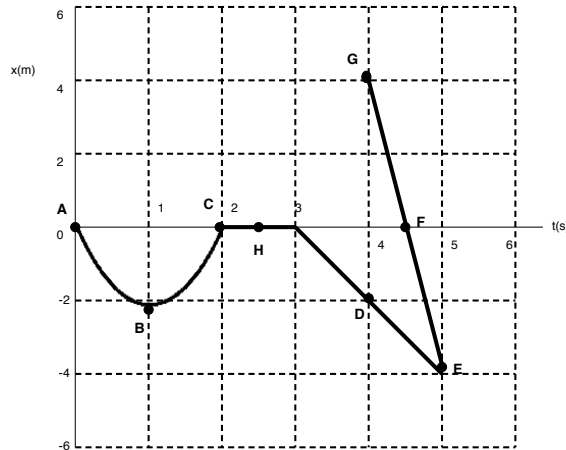


Your Name: _____

**PHY203
Exam #1
Chapters 1-3
Fri., 9/26/14**

Solutions



1. The plot above depicts the position vs. time for the one dimensional motion of a toy car:

a. Find the average velocity (magnitude and sign) from point A to point C.

$$v_{iavg} = \Delta x / \Delta t = (0\text{m} - (0\text{m})) / (2\text{s}) = 0 \quad \mathbf{5}$$

b. Find the instantaneous velocity (magnitude and sign) at point F.

$$v_{int} = \text{slope} = (-8\text{m}) / 1\text{s} = -8.00 \text{ m/s} \quad \mathbf{5}$$

c. Find the average speed (magnitude and sign) from point D to point G.

$$\text{speed}_{iavg} = \Delta s / \Delta t = (10\text{m}) / (0\text{s}) = \text{undefined} \quad \mathbf{5}$$

other reasonable answers are also accepted

d. Find the average acceleration (magnitude and sign) from point H to point F.

$$a_{iavg} = \Delta v / \Delta t = (-8.00\text{m/s} - 0) / (2\text{s}) = -4.00\text{m/s}^2 \quad \mathbf{10}$$

2. Consider a rocket being launched from rest at ground level (height = 0) straight up into the atmosphere. In the first stage, the rocket accelerates at 17.5 m/s^2 for 12.0 s . Then the motor cuts off and the rocket continues to travel upwards for a while. (Ignore any effects due to air resistance.)

a. Find the height of the rocket when the motor cuts off.

$$\begin{aligned} H_1 &= 0 + \frac{1}{2}(17.5 \text{ m/s}^2)(12.0)^2 & \mathbf{5} \\ &= 1260 \text{ m} = 1.26 \times 10^3 \text{ m} \end{aligned}$$

b. Find the speed of the rocket when the motor cuts off.

$$\begin{aligned} v &= 0 + (17.5 \text{ m/s}^2)(12.0 \text{ s}) & \mathbf{5} \\ v &= +210 \text{ m/s} \end{aligned}$$

c. Find the height of the rocket at its highest point.

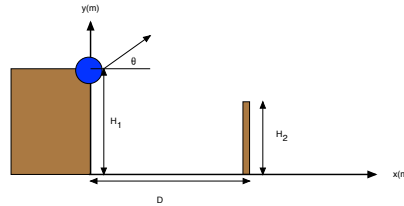
$$\begin{aligned} 0 &= (210)^2 + 2(-9.81)(H_2) \\ H_2 &= 2248 \text{ m} & \mathbf{15} \\ H &= 2248 \text{ m} + 1260 \text{ m} \\ &= 3.51 \times 10^3 \text{ m} \end{aligned}$$

d. Find the time it takes the rocket to reach its highest point.

$$\begin{aligned} 0 &= 210 \text{ m/s} + (-9.81 \text{ m/s}^2)(t_2) & \mathbf{10} \\ t_2 &= 21.4 \text{ s} \end{aligned}$$

$$t = 21.4 \text{ s} + 12.0 \text{ s} = 33.4 \text{ s}$$

3. A cannonball is launched with an angle θ , from the top of a tall building with height H_1 at a nearby wall a distance $D=50.0$ m from the building that has height H_2 . The initial velocity in the y-direction given to the ball is 27.5 m/s. It takes 4.50 s for the cannonball to hit the top of the wall (ignore the thickness of the wall).



a. Find the initial velocity of the ball in the x-direction (magnitude and sign).

$$50.0 \text{ m} = 0 + (v_{0x})(4.50 \text{ s}) \quad \mathbf{10}$$

$$v_{0x} = 11.1 \text{ m/s}$$

b. Find the initial speed of the ball.

$$v_o = \sqrt{(11.1)^2 + (27.5)^2} \quad \mathbf{5}$$

$$= 29.7 \text{ m/s}$$

c. Find the angle the ball made initially with respect to the horizontal (x) direction.

$$\theta = \tan^{-1}\left(\frac{27.5}{11.1}\right) = 68.0^\circ \quad \mathbf{5}$$

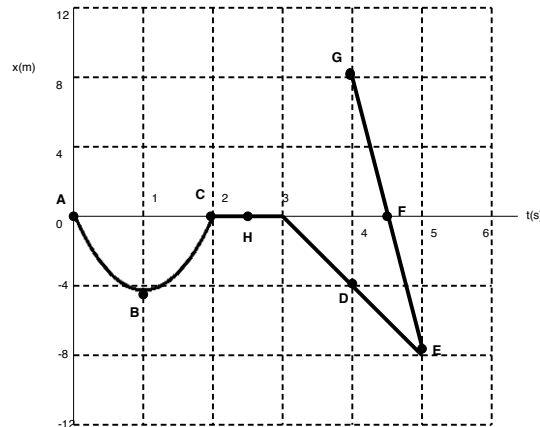
d. Find and write the velocity in vector notation using the coordinate system shown above for when the ball just hits the top of the wall.

$$v_y = 27.5 \text{ m/s} + (-9.81 \text{ m/s}^2)(4.50) \quad \mathbf{15}$$

$$v_y = -16.6 \text{ m/s}$$

$$\mathbf{v} = (11.1\mathbf{i} - 16.6\mathbf{j}) \text{ m/s} \quad \mathbf{5}$$

Alt Version



1. The plot above depicts the position vs. time for the one dimensional motion of a toy car:

a. Find the average velocity (magnitude and sign) from point A to point C.

$$v_{iavg} = \Delta x / \Delta t = (0\text{m} - (0\text{m})) / (2\text{s}) = 0 \quad \mathbf{5}$$

c. Find the instantaneous velocity (magnitude and sign) at point F

$$v_{int} = \text{slope} = (-16\text{m}) / 1\text{s} = -16.0 \text{ m/s} \quad \mathbf{5}$$

c. Find the average speed (magnitude and sign) from point D to point G.

$$\text{speed}_{iavg} = \Delta s / \Delta t = (20\text{m}) / (0\text{s}) = \text{undefined} \quad \mathbf{5}$$

other reasonable answers are also accepted

d. Find the average acceleration (magnitude and sign) from point H to point F.

$$a_{iavg} = \Delta v / \Delta t = (-16.0\text{m/s} - 0) / (2\text{s}) = -8.00\text{m/s}^2 \quad \mathbf{10}$$

2. Consider a rocket being launched from rest at ground level (height = 0) straight up into the atmosphere. In the first stage, the rocket accelerates at 19.5 m/s^2 for 14.0 s . Then the motor cuts off and the rocket continues to travel upwards for a while. (Ignore any effects due to air resistance.)

a. Find the height of the rocket when the motor cuts off.

$$\begin{aligned} H_1 &= 0 + 0 + 1/2(19.5 \text{ m/s}^2)(14.0)^2 && \mathbf{5} \\ &= 1911 \text{ m} = 1.91 \times 10^3 \text{ m} \end{aligned}$$

b. Find the speed of the rocket when the motor cuts off.

$$\begin{aligned} v &= 0 + (19.5 \text{ m/s}^2)(14.0 \text{ s}) && \mathbf{5} \\ v &= +273 \text{ m/s} \end{aligned}$$

c. Find the height of the rocket at its highest point.

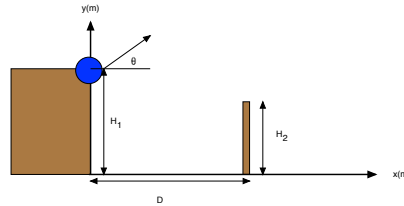
$$\begin{aligned} 0 &= (273)^2 + 2(-9.81)(H_2) \\ H_2 &= 3799 \text{ m} && \mathbf{15} \\ H &= 3799 \text{ m} + 1911 \text{ m} \\ &= 5.71 \times 10^3 \text{ m} \end{aligned}$$

d. Find the time it takes the rocket to reach its highest point.

$$\begin{aligned} 0 &= 273 \text{ m/s} + (-9.81 \text{ m/s}^2)(t_2) && \mathbf{10} \\ t_2 &= 27.8 \text{ s} \end{aligned}$$

$$t = 27.8 \text{ s} + 14.0 \text{ s} = 41.8 \text{ s}$$

3. A cannonball is launched with an angle , θ , from the top of a tall building with height H_1 at a nearby wall a distance $D=60.0$ m from the building that has height H_2). The initial velocity in the y-direction given to the ball is 25.5 m/s. It takes 4.50 s for the cannonball to hit the top of the wall (ignore the thickness of the wall).



a. Find the initial velocity of the ball in the x-direction (magnitude and sign).

$$60.0 \text{ m} = 0 + (v_{0x})(4.50 \text{ s}) \quad \mathbf{10}$$

$$v_{0x} = 13.3 \text{ m/s}$$

b. Find the initial speed of the ball.

$$v_o = \sqrt{(13.3)^2 + (25.5)^2} \quad \mathbf{5}$$

$$= 28.8 \text{ m/s}$$

c. Find the angle the ball made initially with respect to the horizontal (x) direction.

$$\theta = \tan^{-1}\left(\frac{25.5}{13.3}\right) = 62.5^\circ \quad \mathbf{5}$$

d. Find and write the velocity in vector notation using the coordinate system shown above for when the ball just hits the top of the wall.

$$v_y = 25.5 \text{ m/s} + (-9.81 \text{ m/s}^2)(4.50) \quad \mathbf{15}$$

$$v_y = -18.6 \text{ m/s}$$

$$\mathbf{v} = (13.3\mathbf{i} - 18.6\mathbf{j}) \text{ m/s} \quad \mathbf{5}$$