

Your Name: _____

PHY203

Exam #1
Chapters 1-3
Fri., 2/06/09

Solutions

1. How many cubic centimeters is a volume of 3 quarts?

- a. $5.05 \times 10^{-3} \text{ cm}^3$ 3 quarts = 0.75gal x (3.785L/gal)
 b. $1.98 \times 10^2 \text{ cm}^3$ x ($10^3 \text{ cm}^3/\text{L}$) = $2.84 \times 10^3 \text{ cm}^3$
c. $2.84 \times 10^3 \text{ cm}^3$
 d. $5.05 \times 10^3 \text{ cm}^3$
 e. None of the above

For problems 2-5 consider two trains approaching each other from opposite directions on parallel tracks. The measurements start when they are 200m apart. In all cases below, train 1 is traveling to the right and passes the position $x=0$ at $t=0$ traveling in the positive x -direction towards train 2 at a constant speed of 5 m/s. In all cases below, find the x position at which the trains just start to pass each other:

2. Case 1: Train 2 passes the $x=200\text{m}$ position at $t=0$ traveling with a constant speed of 5 m/s.

- a. 50m $x_1 = 5t; x_2 = 200-5t$
 b. 125m $x_1 = x_2 : 5t = 200-5t$
 c. 150m $200 = 10t; t=20\text{s}$
 d. 175m $x=5\text{m/s}(20\text{s}) = 100\text{m}$
e. None of the above (100m)

3. Case 2: Train 2 passes the $x=200\text{m}$ position at $t=0$ traveling with a constant speed of 4 m/s.

- a. 22.2m $x_1 = 5t; x_2 = 200-4t$
 b. 88.9m $x_1 = x_2 : 5t = 200-4t$
c. 111m $200 = 9t; t=22.2\text{s}$
 d. 200m $x=5\text{m/s}(22.2\text{s}) = 111\text{m}$
 e. None of the above

4. Case 3: Train 2 passes the $x=200\text{m}$ position at $t=10\text{s}$ traveling with a constant speed of 4 m/s.

- a. 26.6m $x_1 = 5t; x_2 = 200-4(t-10)$
 b. 71.1m $x_1 = x_2 : 5t = 200-4t+40$
 c. 88.8m $240 = 9t; t=26.6\text{s}$
d. 133m $x=5\text{m/s}(26.6\text{s}) = 133\text{m}$
 e. None of the above

5. Case 4: Train 2 starts from rest at the $x=200\text{m}$ position at $t=5\text{s}$ traveling with a constant magnitude of acceleration of 4 m/s^2 .

- a. 55m $x_1 = 5t; x_2 = 200-1/2(4)(t-5)^2$
b. 66m $x_1 = x_2 : 5t = 200-2(t^2-10t+25)$
 c. 77.6m quad. eq.; $t=13.2\text{s}$
 d. 132m $x=5\text{m/s}(13.2\text{s}) = 66\text{m}$
 e. None of the above

Given the choices above, answer the following questions, 6-10:

6. Given a plot of x vs. t as shown below, which of the graphs above depicts a plot of velocity vs. t : a., **b.**, c., d., or e. none of the above?

7. Given the same plot of x vs. t as shown in #6, which of the graphs above depicts a plot of acceleration vs. t : a., b., c., d., or **e.** none of the above?

8. Given a plot of velocity vs. t as shown below, which of the graphs above depicts a plot of acceleration vs. t : **a.**, b., c., d., or e. none of the above?

9. Given a plot of x vs. t as shown below, which of the graphs above depicts a plot of velocity vs. t : a., b., c., d., or **e.** none of the above?

10. Given a plot of acceleration vs. t as shown below, which of the graphs above depicts a plot of velocity vs. t : a., b., c., **d.**, or e. none of the above?

11. A projectile is shot in a direction 30 degrees below the horizontal from a height of 500m and initial speed of 50m/s, as shown above. (Use $g=9.81\text{m/s}^2$)

a. Write the initial velocity vector, \mathbf{v}_0 , in vector notation, *using the coordinate system given*

above.

$$\mathbf{v}_O = 50 \text{ m/s}(\cos 30^\circ \mathbf{i} + \sin 30^\circ \text{ m/s } \mathbf{j}) = 43.3 \text{ m/s } \mathbf{i} + 25 \text{ m/s } \mathbf{j}$$

b. Calculate the time in sec. that it will take for the projectile to hit the ground.

$$500 \text{ m} = 0 + 25 \text{ m/s } t + 1/2(9.81 \text{ m/s}^2)t^2$$

$$0 = -500 \text{ m} + 25 \text{ m/s } t + 4.905t^2$$

Use quadratic equation; $t = 7.86 \text{ s}$

c. Calculate the x position at which the projectile will hit the ground (the “range”).

$$x = 0 + 43.3 \text{ m/s } (7.86 \text{ s}) = 340.5 \text{ m}$$

d. Calculate the final velocity in the x-direction of the projectile just before it hits the ground, *using the coordinate system given above.*

$$v_X = v_{XO} = +43.3 \text{ m/s}$$

e. Calculate the final velocity in the y-direction of the projectile just before it hits the ground, *using the coordinate system given above.*

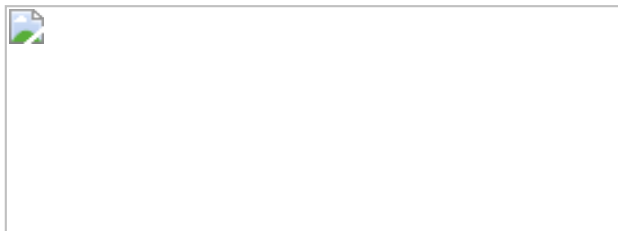
$$v_y = 25 \text{ m/s} + (9.81 \text{ m/s}^2)(7.86 \text{ s}) = +102.1 \text{ m/s}$$

f. Calculate the final speed (just before hitting the ground).

$$v = (43.3^2 + 102.1^2)^{1/2} = 111 \text{ m/s}$$

g. Calculate the final angle the projectile makes with respect to the x-axis (just before hitting the ground) (measured in a clockwise direction).

$$q = \tan^{-1}((102.1/43.3)) = 67^\circ$$



11. A projectile is shot in a direction 60 degrees below the horizontal from a height of 500m and initial speed of 50m/s, as shown above. (Use $g=9.81\text{m/s}^2$)

a. Write the initial velocity vector, \mathbf{v}_O , in vector notation, *using the coordinate system given above.*

$$\mathbf{v}_O = 50 \text{ m/s}(\cos 60^\circ \mathbf{i} + \sin 60^\circ \text{ m/s } \mathbf{j}) = 25 \text{ m/s } \mathbf{i} + 43.3 \text{ m/s } \mathbf{j}$$

b. Calculate the time in sec. that it will take for the projectile to hit the ground.

$$500 \text{ m} = 0 + 43.3 \text{ m/s } t + 1/2(9.81 \text{ m/s}^2)t^2$$

$$0 = -500 \text{ m} + 43.3 \text{ m/s } t + 4.905t^2$$

Use quadratic equation; $t = 6.6 \text{ s}$

c. Calculate the x position at which the projectile will hit the ground (the “range”).

$$x = 0 + 25 \text{ m/s} (6.6 \text{ s}) = 165 \text{ m}$$

d. Calculate the final velocity in the x-direction of the projectile just before it hits the ground, *using the coordinate system given above.*

$$v_x = v_{x0} = +25 \text{ m/s}$$

e. Calculate the final velocity in the y-direction of the projectile just before it hits the ground, *using the coordinate system given above.*

$$v_y = 43.3 \text{ m/s} + (9.81 \text{ m/s}^2)(6.6 \text{ s}) = + 108 \text{ m/s}$$

f. Calculate the final speed (just before hitting the ground).

$$v = (25^2 + 108^2)^{1/2} = 111 \text{ m/s}$$

g. Calculate the final angle the projectile makes with respect to the x-axis (just before hitting the ground) (measured in a clockwise direction).

$$q = \tan^{-1}((108/25)) = 77^\circ$$